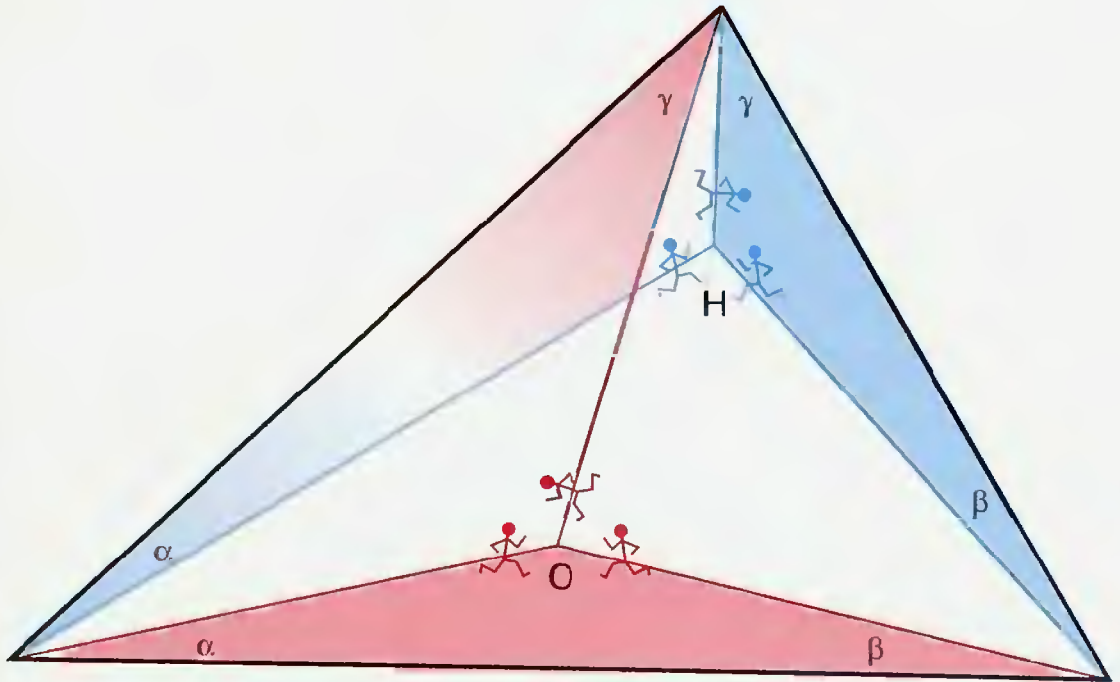


EPISODES IN NINETEENTH AND TWENTIETH CENTURY EUCLIDEAN GEOMETRY



ROSS HONSBERGER



We concur!

*We, equally
inclined, also concur.*

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AND TWENTIETH CENTURY
EUCLIDEAN GEOMETRY**

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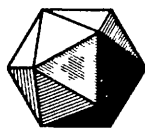
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EUCLIDEAN GEOMETRY**

by

Ross Honsberger

University of Waterloo



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